Graphs and Coloring

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Lecture 7: Discrete Mathematical Modelling

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- For a *directed* graph we consider edges as ordered pairs.

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- $E = \{(1,2), (1,3), (2,3), (2,4)\}$.
- For an unordered graph, the order of the vertices in each edge does not matter.
- $G = \{V, E\}$ is a graph.